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Kevin Woods* (Kevin.Woods@oberlin.edu), Department of Mathematics, Oberlin College, Oberlin, OH 44074. *A Finite Calculus Approach to Ehrhart Polynomials*. Preliminary report.

Given a polytope P , the lattice point enumerator counts, as a function of t , the number of integer points in the dilated polytope tP . If P has rational vertices, this function is a quasi-polynomial in t , called the Ehrhart quasi-polynomial. Inspired by the analogy of Ehrhart quasi-polynomials as a discrete version of the volume of a polytope, we present a new proof of the existence of these quasi-polynomials. This proof uses finite calculus and induction, and provides quick proofs of two other related results: McMullen's theorem about the periods of the individual coefficients of the quasi-polynomial, and the Ehrhart-Macdonald theorem on reciprocity. This is joint work with Steven Sam. (Received March 03, 2009)