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**John Wermer\***, Department of Mathematics, Brown University, Providence, RI. *A Cauchy-Riemann equation for generalized analytic functions.*

In (1), "Generalized Analytic Functions", TAMS 81 (1956), R. Arens and I. Singer studied the following generalization of the disk algebra.  $T^2$  is the 2-torus and  $\alpha$  is a positive irrational number.  $A_\alpha$  is the algebra of all continuous functions on  $T^2$  with Fourier coefficients in the half-plane  $|n + m\alpha| \geq 0$ . The maximal ideal space of  $A_\alpha$  identifies with the set  $M$  of  $(z, w) \mid |w| = |z|^\alpha, |z| \leq 1$  in  $C^2$ . Helson and Lowdenslager in 1959 developed a rich theory of  $A_\alpha$ . Define the differential operator  $X = \bar{z}\delta_{\bar{z}} + \alpha\bar{w}\delta_{\bar{w}}$  on  $C^2$ .  $X$  is well-defined on the 3-manifold  $M$ . (0, 0). Using results in (1), we prove Theorem:  $A_\alpha$  consists of all  $f$  in  $C(T^2)$  which have a continuous extension  $F$  to  $M$  such that  $X(F) = 0$  in the sense of distributions on  $M$  minus (0, 0). (Received February 12, 2009)