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Marius Beceanu*, 5734 S. University Ave., University of Chicago Mathematics Department,
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Consider the $H^{1/2}$ -critical Schrödinger equation with a cubic nonlinearity in \mathbb{R}^3

$$i\partial_t\psi + \Delta\psi + |\psi|^2\psi = 0.$$

It admits an eight-dimensional manifold of periodic solutions called solitons

$$e^{i(\Gamma+vx-t|v|^2+\alpha^2t)}\phi(x-2tv-D, \alpha),$$

where $\phi(x, \alpha)$ is a positive ground state solution of the semilinear elliptic equation

$$-\Delta\phi + \alpha^2\phi = \phi^3.$$

We prove that in the neighborhood of the soliton manifold there exists a $H^{1/2}$ Lipschitz manifold N of asymptotically stable solutions of the equation, meaning they are the sum of a moving soliton and a dispersive term.

Furthermore, a solution starting on N remains on N for all positive time and for some finite negative time and N can be identified as the centre-stable manifold for this equation.

The proof is based on the method of modulation, introduced by Soffer and Weinstein and adapted by Schlag to the L^2 -supercritical case.

The main result depends on a spectral assumption concerning the absence of embedded eigenvalues.

New estimates for the time-dependent and time-independent linear Schrödinger equation are also established. (Received February 26, 2009)