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Ning Ju* (ningju@math.okstate.edu), Department of Mathematics, Oklahoma State University, 401 Mathematical Sciences, Stillwater, OK 74078. *Global Wellposedness for the 2D Boussinesq Equations with Fractional Dissipation.*

Consider the following initial value problem of the two dimensional Boussinesq equation with fractional dissipation:

$$\left\{ \begin{array}{l} \partial_t v + (v \cdot \nabla)v = -\nabla p + \theta e_2 - \nu \Lambda^{2\beta} v, \quad \Lambda = (-\Delta)^{\frac{1}{2}}, \\ \nabla \cdot v = 0, \\ \theta_t + v \cdot \nabla \theta = -\kappa \Lambda^{2\alpha} \theta, \\ v(\cdot, 0) = v_0, \\ \theta(\cdot, 0) = \theta_0. \end{array} \right.$$

where $v(x, t)$ is the velocity vector field of the incompressible fluid, $\theta(x, t)$ is the fluid temperature, p is the fluid pressure and e_2 is the vector $(0, 1)$ in the physical domain. The parameters $\alpha, \beta \in [0, 1)$, $\nu, \kappa > 0$ are constants.

We prove existence and uniqueness of the global (in time) strong solution to the above Cauchy problem in Sobolev space for $\alpha \geq \frac{1}{2}$ and $\beta \geq \frac{1}{2}$. Other related issues will also be discussed. (Received March 03, 2009)