

1049-46-102

**Osamu Hatori\*** ([hatori@math.sc.niigata-u.ac.jp](mailto:hatori@math.sc.niigata-u.ac.jp)). *Isometries between the groups of invertible elements in Banach algebras.*

We will consider a problem that isometries between the groups of invertible elements of Banach algebras induces isometrical real algebra isomorphisms. In particular, we show that for certain Banach algebras  $A$  (commutative) and  $B$  if  $T$  is a surjective isometry from  $A^{-1}$  onto  $B^{-1}$ , then  $T/T(1)$  is an isometrical real algebra isomorphism. Thus we see that  $A^{-1}$  and  $B^{-1}$  are isometric as a metric space if and only if  $A^{-1}$  and  $B^{-1}$  are isometrically isomorphic as metrizable groups. (Received March 02, 2009)