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**Lourdes Palacios\*** (pafa@xanum.uam.mx), Avenida San Rafael Atlixco 186, Colonia Vicentina, 09340 Mexico City, Mexico. *On some  $Q$ -like properties in Topological Algebras.* Preliminary report.

In a unital Banach algebra  $A$  the set  $G(A)$  of its invertible elements is an open set and the application  $x \rightarrow x^{-1}$  from  $G(A)$  onto  $G(A)$  is continuous. More generally, if  $A$  is a metrizable and complete topological algebra, then the mapping  $x \rightarrow x^{-1}$  is continuous if and only if  $G(A)$  is a  $G_\delta$  set.

We say that a topological algebra  $A$  is a  $Q$ -algebra if the set  $G(A)$  is an open set. If  $A$  is a commutative  $Q$ -algebra and the mapping  $x \rightarrow x^{-1}$  is continuous, i.e. it is a Waelbroeck algebra, then all the maximal ideals are closed and of codimension 1

$Q$ -topological algebras have some interesting properties as the following: the spectrum  $\sigma(x)$  is compact for every  $x \in A$  and if  $A$  is commutative, then the set  $\mathfrak{M}(A)$  of all non-zero linear, multiplicative and continuous functionals of  $A$  is non empty if and only if  $A$  is not a field and  $A$  is a *Gelfand-Mazur algebra*.

We will examine some properties related to  $Q$ -algebras and their relations with some other algebras. We will also provide some interesting examples. (Received March 01, 2009)