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Ji-A Yeum* (yeum@math.ohio-state.edu), Ohio State University, Department of mathematics, 231 W 18th Avenue, Columbus, OH 43210. *Probability of solvability of random systems of 2-linear equations over $GF(2)$.*

We consider the random system of 2-linear equations over the finite field $GF(2)$ whose left hand side corresponds to the random graph $G(n, p)$ and whose right hand side consists of independent Bernoulli random variables with success probability $1/2$, assuming that the right hand side is independent of the left hand side.

$G(n, p)$ is the random graph with n labeled vertices such that each of the $\binom{n}{2}$ possible edges is present in the graph independently of all others, with probability p .

We prove that when $G(n, p)$ is at the subcritical phase and $|\lambda| \gg n^{1/39}$, $|\lambda| = O(n^{1/12-\epsilon})$ with a fixed $0 < \epsilon < 1/12 - 1/39$, the probability of solvability of the random system corresponding to $G(n, p)$ is asymptotic to $e^{3/8}|\lambda|^{1/4}n^{-1/12}$ as $n \rightarrow \infty$. Also, we prove that when $G(n, p)$ is at the critical phase, the probability of solvability of the random system corresponding to $G(n, p)$ is asymptotic to $c_\lambda n^{-1/12}$ as $n \rightarrow \infty$, where the constant c_λ is expressed as a convergent double series depending on λ . (Received January 05, 2009)