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**Mikhail H Klin, Dale M Mesner and Andrew J Woldar\*** (andrew.woldar@villanova.edu),  
Department of Mathematical Sciences, Villanova University, Villanova, PA 19085. *The  
Combinatorics of Transitive Extensions.*

If  $(H, \Omega)$  is a permutation group then  $H$  admits natural actions on the sets  $\Omega^k, \Omega^{\{k\}}$  of ordered and unordered  $k$ -tuples, respectively. Hence these sets partition into  $H$ -orbits. We propose an algebraic calculus for partitions of  $\Omega^k, \Omega^{\{k\}}$  which serves to approximate  $H$ -orbit partitions in pure combinatorial terms. In this sense we attempt to formulate combinatorially what it means for a structure to be highly symmetric without saying that its symmetry groups have the property of being highly transitive. Our motivation stems from the way in which association schemes analogously approximate 2-orbits of transitive permutation groups (this is the case  $k = 2$ ). New combinatorial structures are defined, and results which apply these structures to the problem of transitive extension are provided. (Received February 22, 2009)