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**Álvaro Lozano-Robledo\*** (alozano@math.uconn.edu), 196 Auditorium Rd., Dept. of Math., U-3009, University of Connecticut, Storrs, MA 06269. *Bernoulli-Hurwitz numbers, Wieferich primes and Galois representations.*

Let  $K$  be a quadratic imaginary number field with discriminant  $D_K \neq -3, -4$  and class number one. Fix a prime  $p \geq 7$  which is unramified in  $K$ . Given an elliptic curve  $A/\mathbb{Q}$  with complex multiplication by  $K$ , let  $\overline{\rho}_A: \text{Gal}(\overline{K}/K(\mu_{p^\infty})) \rightarrow \text{SL}(2, \mathbb{Z}_p)$  be the representation which arises from the action of Galois on the Tate module. We will show that, for all but finitely many inert primes  $p$ , the image of a certain deformation  $\rho_A: \text{Gal}(\overline{K}/K(\mu_{p^\infty})) \rightarrow \text{SL}(2, \mathbb{Z}_p[[X]])$  of  $\overline{\rho}_A$  is “as large as possible”, that is, it is the full inverse image of a Cartan subgroup of  $\text{SL}(2, \mathbb{Z}_p)$ . If  $p$  splits in  $K$ , then the same result holds as long as certain Bernoulli-Hurwitz number is a  $p$ -adic unit which, in turn, is equivalent to a prime ideal not being a Wieferich place. The proof rests on the theory of elliptic units of Robert and Kubert-Lang, and on the two-variable main conjecture of Iwasawa theory for quadratic imaginary fields. (Received February 26, 2009)