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**Brandt Kronholm\*** (jk174783@albany.edu), Earth Science and Mathematics 110, 1400  
Washington Avenue, Albany, NY 12222. *Ramanujan Congruence Properties of the Restricted  
Partition Function  $p(n, m)$ .*

The restricted partition function  $p(n, m)$  enumerates the number of partitions of  $n$  into exactly  $m$  parts. The relationship between the unrestricted partition function  $p(n)$  and  $p(n, m)$  is clear:

$$p(n) = p(n, 1) + p(n, 2) + \dots + p(n, n).$$

We are all familiar with Ramanujan's partition congruences for  $p(n)$  and that Ken Ono (2000) proved that there are Ramanujan congruences for  $p(n)$  for every prime  $\ell > 3$ . In 2005 the speaker showed that there are Ramanujan congruences for  $p(n, m)$  for every prime  $m = \ell \geq 3$ . However, given our choice of prime  $\ell$  for both  $p(n)$  and  $p(n, m)$ ,  $n$  is restricted to a very special form. For example, if  $\ell = 5$ , then we are guaranteed that  $p(n) \equiv 0 \pmod{5}$  when  $n = 5k + 4$ . We are likewise guaranteed for  $\ell = 5$  that  $p(n, 5) \equiv 0 \pmod{5}$  when  $n = 60k$  and  $n = 60k - 5$ .

In this talk we will discuss a Ramanujan-like congruence relation for  $p(n, m)$  where for our choice of prime  $\ell$  there is no restriction on  $n$ . (Received August 25, 2009)