

1052-13-134

**Timothy B.P. Clark\*** (tbpc Clark@math.northwestern.edu), Mathematics Department, 2033 Sheridan Road, Evanston, IL 60208. *Poset resolutions of monomial ideals.*

Let  $P$  be a finite partially ordered set (poset) with set of atoms  $A$  and let  $k$  be a field. Considering certain open intervals of  $P$ , we utilize a construction of Tchernev to produce a sequence of  $k$ -vector spaces and vector space maps  $\mathcal{D}(P)$ . When a poset map  $\eta : P \rightarrow \mathbb{Z}^n$  exists, the sequence  $\mathcal{D}(P)$  is homogenized to approximate a free resolution  $\mathcal{F}(\eta)$  of  $R/N$  where  $N$  is the monomial ideal in  $k[x_1, \dots, x_n]$  whose set of minimal generators is  $\{x^{\eta(a)} : a \in A\}$ . When  $\mathcal{F}(\eta)$  is an exact complex of multigraded modules, we call it a *poset resolution* of  $R/N$ . We show that the poset which provided our original motivation, the lcm-lattice associated to  $N$ , supports the minimal free resolution for a class of ideals we call *lattice-linear*. This class of monomial ideals contains both the class of ideals with a linear resolution and the class of Scarf ideals. More generally, poset resolutions provide a common framework from which to view a number of (not necessarily minimal) resolutions previously constructed using distinct methods. Specifically, we show that both the Taylor resolution and Eliahou-Kervaire minimal resolution may be viewed as poset resolutions. (Received August 26, 2009)