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1118 E. 58th Street, Chicago, IL 60637. *Six model structures for DG modules over DGA's.*

Let  $A$  be a differential graded algebra over a commutative ring  $R$  and let  $M(A)$  be the category of differential graded (left)  $A$ -modules. There are three obvious notions of weak equivalence in  $M(A)$ :  $A$ -homotopy equivalence,  $R$ -homotopy equivalence, and quasi-isomorphism. These lead to three triangulated categories. There are (at least) six sensible model category structures on  $M(A)$ , one, two, and three, respectively, for the three kinds of weak equivalences just named. In one of them, the classical bar construction  $B(A,A,X)$  is a model theoretic cofibrant approximation of  $X$ . All of these model structures seem natural and interesting. There appear to be many other contexts in algebra and topology where such a sextet of interrelated model structures is present. (Received August 23, 2009)