

1052-20-76

**Gareth A. Jones\*** ([G.A.Jones@maths.soton.ac.uk](mailto:G.A.Jones@maths.soton.ac.uk)), School of Mathematics, University of Southampton, Highfield, Southampton, Hampshire SO17 1BJ, England. *Beauville surfaces and finite groups.*

Beauville surfaces are 2-dimensional complex algebraic varieties which are rigid in the sense of having no deformations. They can be constructed as quotients  $(C_1 \times C_2)/G$  where  $C_1$  and  $C_2$  are compact Riemann surfaces of genus at least 2, with a group  $G$  acting as automorphisms of each so that it acts freely on  $C_1 \times C_2$ , and so that  $C_i \rightarrow C_i/G$  is a covering of the Riemann sphere branched over three points (i.e. each  $C_i$  admits a regular dessin with automorphism group  $G$ ). Bauer, Catanese and Grunewald have conjectured that every non-abelian finite simple group  $G$ , except  $A_5$ , acts in such a way. Extending their results and those of Fuertes and González-Diez, I shall verify this for the simple groups  $L_2(q)$ , the Suzuki groups  $Sz(2^e)$ , the Ree groups  $R(3^e)$ , and the quasi-simple groups  $SL_2(q)$ ,  $q > 5$ . (Received August 20, 2009)