

1052-39-26

Harry Gingold* (gingold@math.wvu.edu), WVU, Department of Mathematics, Armstrong Hall, Morgantown, WV 26506. *COMPACTIFICATION AND BLOW UP OF SOLUTIONS IN NONLINEAR FINITE DIFFERENCE SYSTEMS*. Preliminary report.

Abstract. Nonlinear systems of difference equations are studied via a new compactification method that distinguishes among different directions at infinity. This compactification transforms a polynomial system in \mathbb{R}^n , to a rational system inside the unit ball. On the unit ball, of the compactified system, a family of solutions that correspond to ideal solutions of the original polynomial equation in \mathbb{R}^n is defined. The compactification allows us to define critical points at infinity. The critical points at infinity lead to a nonlinear eigenvalue problem. If a critical point on the boundary of the compactified system is "hyperbolic", then the original system is expected to possess solutions that blow up. A naive expectation that the Jacobian, about a point $y = \infty$ of any polynomial difference system, solely depends on the highest degree non linear terms of f , is shown to be false. (Received July 14, 2009)