

1053-60-17

David Nualart* (nualart@math.ku.edu), The University of Kansas, Department of Mathematics, Lawrence, KS 66045. *Stochastic differential equations driven by a fractional Brownian motion with any Hurst parameter.*

We introduce a new method to construct a rough path above a d -dimensional fractional Brownian motion B^H with any Hurst parameter $H \in (0, 1)$. This method has been inspired by the approach of J. Unterberger, and it is based on the representation of the fractional Brownian motion as a Volterra Gaussian process

$$B_t^H = \int_0^t K_H(t, s) dW_s,$$

where $\{W_t\}$ is a d -dimensional standard Wiener process. The main idea is to define iterated integrals

$$\int_{s < u_1 < \dots < u_n < t} dB_{u_1}^{H, i_1} \dots dB_{u_n}^{H, i_n}$$

for $0 \leq s < t \leq T$, $n \leq [1/H]$ and $i_1, \dots, i_n \in \{1, \dots, d\}$, in such a way that they satisfy the required properties of Hölder continuity, multiplicativity and geometricity. A compact and simple formula for these iterated integrals is given. The method can be extended to a general class of Gaussian Volterra processes. We will discuss how this construction allows us to solve stochastic differential equations driven by a fractional Brownian motion with any Hurst parameter. This is a joint work with Samy Tindel. (Received May 26, 2009)