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**Hung-ping Tsao\*** (hptsao@hotmail.com), 1151 Highland Drive, Novato, CA 94949. *Expressing the  $k$ th power sum of the nature numbers as a polynomial in the first power sum.*

Set  $S=S(1)$ , where  $S(k)$  is the sum of the  $k$ th powers of  $1, 2, 3, \dots, n$ . It is well-known that  $S(3)$  is the square of  $S$ , namely  $CS(3)=(1,0,0)$ , where  $CS(2k-1)$  is the coefficient  $(k+1)$ -tuple of the polynomial in  $S$  for  $S(2k-1)$ . From  $CS(5)=(4/3, -1/3, 0, 0)$ ,  $CS(7)=(2, -4/3, 1/3, 0, 0)$ ,  $CS(9)=(16/5, -4, 12/5, -3/5, 0, 0)$ ,  $CS(11)=(16/3, -32/3, 34/3, -20/3, 5/3, 0, 0), \dots$ , we form a triangular array TO. We also have  $S(4)/S(2)=(6/5)S-1/5$ . Let  $C(S(2k)/S(2))$  denote the coefficient  $(k-1)$ -tuple of the polynomial in  $S$  for  $S(2k)/S(2)$ . From  $C(S(6)/S(2))=(12/7, -6/7, 1/7)$ ,  $C(S(8)/S(2))=(8/3, -8/3, 6/5, -1/5)$ ,  $C(S(10)/S(2))=(48/11, -80/11, 68/11, -30/11, 5/11), \dots$ , we form another triangular array TE. Among other things, we found a keen relationship between TO and TE. (Received June 22, 2009)