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Jozsef Solymosi* (solymosi@math.ubc.ca), 1984 Mathematics Road, Vancouver, BC. V6T1Z2, Canada, and **Endre Szemerédi**. *On sumsets which have large subsets with small doubling*. Preliminary report.

Let A be a finite subset of an abelian group. The sumset $A + A$ is the set of all pairwise sums $a + b$ where a and b are elements of A . One of the central results in additive combinatorics is Freiman's theorem which describes the structure of sets with small sumsets. In this talk we consider the following problem; suppose that $|A + A| \leq |A|^{3/2}$. Under what conditions can we guarantee that a large subset $B \subset A + A$ has small doubling? (i.e. $|B + B| \leq C|B|$ where C is a slow-growing function of $|B|$) We will see that this is the case when A is uniform enough. We will illustrate the result with applications to the sum-product conjecture and some related problems. (Received September 15, 2009)