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Spain. *Classifying t -structures in Commutative Algebra.*

In this talk we will present our results on t -structures on the derived category of modules over a commutative noetherian ring R , developed jointly with Alonso and Saorín. A theorem of Hopkins and Neeman classifies triangulated t -structures a.k.a. Bousfield localizations, they are in bijection with subsets of $\text{Spec}(R)$. As it was shown by Stanley, this classification is impossible for general t -structures because they form a proper class already for \mathbb{Z} . We will treat the case of *compactly generated* t -structures. They are classified by decreasing filtrations by supports of $\text{Spec}(R)$. All t -structures on $\mathbf{D}_{fg}^b(R)$, the subcategory of bounded complexes with finite type homology, is the restriction of a compactly generated t -structure on $\mathbf{D}(R)$. A decreasing filtration by supports $\phi: \mathbb{Z} \rightarrow \text{Spec}(R)$ satisfies the weak Cousin condition (wCc) if $\phi(i)$ contains all immediate generalizations of the points of $\phi(i+1)$. Every t -structure on $\mathbf{D}_{fg}^b(R)$ is induced by a compactly generated t -structure on $\mathbf{D}(R)$ whose associated filtration by supports satisfies wCc and these are all if R has a dualizing complex. (Received January 26, 2010)