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**Pietro Poggi-Corradini\***, Department of Mathematics, Cardwell Hall, Kansas State University, Manhattan, KS 66506. *Evolution of analytic Jordan curves under conformal maps of an annulus*. Preliminary report.

Let  $f$  be an analytic map near 0 with  $f(0) = 0$  and  $f'(0) \neq 0$ . For  $r$  fixed (small)  $f(re^{i\theta})$  describes an analytic Jordan curve  $J(r)$ , and hence defines an inner domain  $G_1$  and an outer domain  $G_2$ . Let  $M_1(r)$  be the reduced modulus of  $J(r)$  with respect to 0 in  $G_1$ , and let  $M_2(r)$  the reduced modulus of  $J(r)$  with respect to  $\infty$  in  $G_2$ . Then  $M_1(r) + M_2(r) \leq 0$  with equality if and only if  $J(r)$  is a circle centered at 0. Teichmüller's famous *Modulsatz* states that if  $M_1 + M_2$  is close to 0, then  $J$  is closed to being a circle (geometrically). So the quantity  $M_1 + M_2$  can be thought as a measure of how far  $J$  is from being a circle. In previous work we showed that  $|M_1(r) + M_2(r)|$  is monotonically increasing with  $r$ . Inspired by the recent breakthrough of Iwaniec, Kovalev, and Onninen on the Nitsche conjecture, we have extended our result to conformal mappings defined on an annulus  $\{1 < |z| < R\}$  such that  $|f(z)| = 1$  for  $|z| = 1$ . We will finish the talk with some open problems related to the work of Pólya and Szegő. (Received January 04, 2010)