For each $\alpha \in (0, 1)$, we construct a manifold with an $\alpha$-Hölder continuous almost complex structure, such that the Kobayashi-Royden pseudonorm is not upper semicontinuous. This generalizes an example due to Ivashkovich, Pinchuk, and Rosay, with $\alpha = \frac{1}{2}$. The main idea in the construction is an analysis of complex valued functions $f$ on the unit disk satisfying $\partial f / \partial \bar{z} = |f|^\alpha$. (Received January 09, 2010)