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Michael W. Frazier* (frazier@math.utk.edu), Mathematics Department - 104 Aconda Court, 1534 Cumberland Ave, University of Tennessee, Knoxville, TN 37996-0614, and **Fedor Nazarov** and **Igor E. Verbitsky**. *Global Estimates for Kernels of Neumann Series, Green's Functions, and the Conditional Gauge*. Preliminary report.

We consider estimates for kernels of resolvent series $(I - T)^{-1} = \sum_{j=0}^{\infty} T^j$, for integral operators of the form $Tf(x) = \int_{\Omega} K(x, y)f(y) d\omega(y)$, where (Ω, ω) is a σ -finite measure space, $K : \Omega \times \Omega \rightarrow (0, \infty]$ is symmetric and measurable, $1/K$ satisfies a quasi-metric condition, and $\|T\|_{L^2(\omega) \rightarrow L^2(\omega)} < 1$. Let K_j denote the kernel of T^j . Then there exists $c > 0$ depending only on the quasi-metric constant κ and $C > 0$ depending only on κ and $\|T\|$ such that

$$K(x, y)e^{cK_2(x, y)/K(x, y)} \leq \sum_{j=1}^{\infty} K_j(x, y) \leq K(x, y)e^{CK_2(x, y)/K(x, y)}.$$

We apply this result to obtain estimates for Green's functions associated with fractional Schrödinger operators $(-\Delta)^{\alpha/2} - q$, for $q \geq 0$ and $0 < \alpha \leq 2$, on a domain Ω which could be all of \mathbb{R}^n or a bounded domain in \mathbb{R}^n which satisfies the boundary Harnack principle. These estimates are equivalent to estimates for the conditional gauge for α -stable processes. (Received January 18, 2010)