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This talk presents recent results on the global regularity of classical solutions to the 2D Boussinesq equations with vertical dissipation and vertical thermal diffusion. We prove that the L^r -norm of the vertical velocity v for any $1 < r < \infty$ is globally bounded and that the L^∞ -norm of v controls any possible breakdown of classical solutions. In addition, we show that an extra thermal diffusion given by the fractional Laplace $(-\Delta)^\delta$ for $\delta > 0$ would guarantee the global regularity of classical solutions. (Received January 12, 2010)