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Dmitry Bredikhin* (bredikhin@mail.ru), Lermontova 7-22, Saratov, AS 410002, Russia. *On algebras of relations with operations of cylindrification*. Preliminary report.

Let $Q\{\Omega, \subset\}$ be the quasivariety generated by partial ordered algebras of binary relations whose operations are members of Ω . We shall consider the operations of relation product \circ and two unary operations of cylindrification ∇_1, ∇_2 [1].

Theorem. An partial ordered algebra $(A, \cdot, *, \bullet, \leq)$ of the type $(2, 1, 1)$ belongs to the quasivariety $Q\{\circ, \nabla_1, \nabla_2, \subset\}$ if and only if it satisfies the identities:

$(xy)z = x(yz)$, $(x^*)^\bullet = (x^\bullet)^*$, $x^*y = xy^\bullet$, $(x^*)^* = x^*$, $(x^*)^2 = x^*$, $(xy)^* = xy^*$, $xy^*x^* = xy^*$, $x^*y^*z^* = x^*z^*y^*$, $x^*y^*zy = x^*zy$, $(x^\bullet)^\bullet = x^\bullet$, $(x^\bullet)^2 = x^\bullet$, $(xy)^\bullet = x^\bullet y$, $x^\bullet y^\bullet x = y^\bullet x$, $x^\bullet y^\bullet z^\bullet = y^\bullet x^\bullet z^\bullet$, $xyx^\bullet z^\bullet = xyz^\bullet$, $x \leq x^*$, $x \leq x^*x$, $x^*y \leq x$, $x \leq x^\bullet$, $x \leq xx^\bullet$, $xy^\bullet \leq y$.

[1] L. Henkin, J.D. Monk, A. Tarski. Cylindric algebras I, II. North-Holland, Amsterdam, 1971, 1985. (Received December 01, 2009)