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**Joel Berman\***, Department of Mathematics, University of Illinois at Chicago, 851 S. Morgan Street, Chicago, IL 60607. *Pattern operations, strict pattern operations, and varieties*. Preliminary report.

For  $\alpha$  an equivalence relation on  $\{1, \dots, n\}$ , for  $\bar{a} \in A^n$ , and  $1 \leq k \leq n$  we say  $\bar{a}$  has an  $\alpha$ -*pattern* if  $(i, j) \in \alpha$  implies  $a_i = a_j$  and we call  $(\alpha, k)$  a *pattern pair*. For  $f : A^n \rightarrow A$  and  $\Gamma$  a set of pattern pairs,  $f$  is a  $\Gamma$ -*pattern operation* if  $f(\bar{a}) = a_k$  whenever  $\bar{a} \in A^n$  has an  $\alpha$ -pattern for an  $(\alpha, k) \in \Gamma$ .

A set  $\Gamma$  of pattern pairs is *consistent* if at least one  $\Gamma$ -pattern operation exists. A *strict pattern operation* is defined analogously starting from the definition  $\bar{a} \in A^n$  has a *strict  $\alpha$ -pattern* precisely if  $(i, j) \in \alpha$  iff  $a_i = a_j$ .

Familiar examples of pattern operations include  $n$ -ary near-unanimity operations and Mal'cev operations; examples of strict pattern operations are discriminator and dual-discriminator operations.

For a variety  $\mathcal{V}$  generated by a set  $K$  of algebras, we investigate conditions on  $K$  and  $\mathcal{V}$  that guarantee for a given  $n$ , for every consistent set  $\Gamma$  of [strict] pattern pairs there exists a term  $t_\Gamma$  for which  $t_\Gamma^{\mathbf{A}}$  is a [strict]  $\Gamma$ -pattern operation for all  $\mathbf{A} \in K$ . (Received November 30, 2009)