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The Minimum Rank Problem for Outerplanar Graphs. Preliminary report.

Given a simple graph $G = (V, E)$ on n vertices and a field F , let $S^F(G)$ equal the set of symmetric $n \times n$ F -valued matrices A such that $a_{ij} \neq 0$ iff $ij \in E, i \neq j$. The minimum rank of a graph G over F is equal to $\min\{\text{rank}(A) | A \in S^F(G)\}$. The minimum rank problem of a simple graph G over a field F is to determine the minimum rank of a matrix in $S^F(G)$. The inverse inertia problem of a simple graph G asks which inertias can be obtained by matrices in $S^{\mathbb{R}}(G)$.

A cover for a graph G is a collection of subgraphs of G such that every edge and vertex of G lie in at least one of the subgraphs in the collection. A graph G is outerplanar if there exists a planar drawing of G such that every vertex lies on the outer face of G . We discuss previous results concerning outerplanar graphs and show that every outerplanar graph G has a clique, star, cycle cover such that the sum of the minimum ranks of the graphs in the cover is equal to the minimum rank of G . We discuss corollaries to this result which have implications for determining the positive semi-definite minimum rank and the inertia of an outerplanar graph. (Received February 16, 2010)