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**Uwe Kaiser\*** ([kaiser@math.boisestate.edu](mailto:kaiser@math.boisestate.edu)), Department of Mathematics, 1910 University Drive, Boise, ID 83725-1555. *Commutative Frobenius Algebras and 3-dimensional Compression Bordisms*. Preliminary report.

Given a commutative Frobenius algebra  $V$  over a commutative ring  $R$  with 1 we construct certain  $V^{\otimes j}$ -module categories  $V[j]$  for  $j \geq 0$ . Let  $(M, \alpha)$  be an oriented 3-manifold with a closed oriented 1-manifold  $\alpha$  in its boundary. Then there are defined natural functors from a category of oriented surfaces in  $M$  bounding  $\alpha$  and morphisms defined by *compression bordisms in  $M \times I$* , taking values in  $V[[\alpha]]$ . (Here a compression bordism  $S_1 \rightarrow S_2$  is a 3-dimensional manifold with corners, properly embedded in  $M \times I$ , which is a product over  $\alpha$ , and with only embedded 2-handles and 3-handles attached to  $S_1 \times I$ , considered up to isotopy through those bordisms). The colimit of this functor is the Bar-Natan skein module defined for  $(M, \alpha)$  and the Frobenius algebra  $V$ . Moreover, a glueing theorem can be proven for this functor. The above construction can be twisted with a  $(3 + 1)$ -dimensional TQFT over  $R$  to define functors on a category with the morphisms embedded in oriented 4-manifolds. We discuss the above constructions and some conjectures related to it. (Received February 15, 2010)