We will discuss Hardy-Sobolev spaces on a Riemannian manifold with a doubling measure, and show that the definitions given by means of atomic decomposition and by means of various maximal functions give the same space, which can be identified with the Hajlasz Sobolev space for $p = 1$, provided we assume a Poincare inequality. (Received February 23, 2010)