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Rod Freed* (gauss12@hotmail.com), 12939 Bonaparte #7, Marina Del Rey, CA 90066. *Green's Function and the Inverse of a Differential Operator.*

Let $L^2_m([0, \infty))$ denote the space of L^2 functions on $[0, \infty)$ into C_m , and let F be the differential operator in $L^2_m([0, \infty))$ associated with $f'(t) = Df(t)$, where $f(0)$ is in B , a subspace of C_m . We prove that D has no eigenvalues on the imaginary axis and that C_m is a direct sum of $\text{Ker}(R)$ and B (where R is the Riesz projection of D corresponding to the eigenvalues of D in the open left half plane) if and only if F is invertible. Also, we show that the inverse, $G(h)$, of F is the operator which is the integral of $g(t,s)h(s)$ with respect to s , where $g(t,s)$ is $\exp(-tD)(I-P)\exp(sD)$ for $s < t$ and is $-\exp(-tD)P \exp(sD)$ for $t < s$, where P is the projection of C_m along $\text{Ker}(R)$ onto B . (Received February 18, 2010)