

1060-22-79

Donald R King* (d.king@neu.edu), 567 Lake Hall, Northeastern University, Boston, MA, MA 02115. *Spherical nilpotent orbits and asymptotics of K -types of Harish Chandra modules.*

Let G be the adjoint group of a semisimple Lie algebra \mathfrak{g} and K be a maximal compact subgroup. Let $\mathfrak{p}_{\mathbb{C}}$ be the complexification of the complement of \mathfrak{k} in \mathfrak{g} . $K_{\mathbb{C}}$, the complexification of K , acts on $\mathfrak{p}_{\mathbb{C}}$. $\mathfrak{g}_{\mathbb{C}}$ is the complexification of \mathfrak{g} . Let $e \in \mathfrak{p}_{\mathbb{C}}$ be nilpotent, and set $\mathcal{O} = K_{\mathbb{C}} \cdot e$, the corresponding $K_{\mathbb{C}}$ -orbit. $\overline{\mathcal{O}}$ denotes the Zariski closure of \mathcal{O} . $R[\overline{\mathcal{O}}]$ denotes the ring of regular functions on $\overline{\mathcal{O}}$. Assume that e has height 2. Then \mathcal{O} is a spherical $K_{\mathbb{C}}$ variety and the subring of highest weight vectors in $R[\overline{\mathcal{O}}]$ is a polynomial ring. Let f_1, \dots, f_r be a set of generators with highest weights μ_1, \dots, μ_r . Suppose that \mathbf{X} is an irreducible $(\mathfrak{g}_{\mathbb{C}}, K)$ module whose associated variety is $\overline{\mathcal{O}}$. We show that the asymptotic directions of the K -types of \mathbf{X} are determined by the weights μ_i . (Received March 21, 2010)