

1062-05-107

**Boris G Pittel\*** ([bgp@math.ohio-state.edu](mailto:bgp@math.ohio-state.edu)), Boris Pittel, Columbus, OH 43221. *Tight Markov chains and random compositions.*

For an ergodic Markov chain  $\{X(t)\}$  on  $\mathbb{N}$ , with a stationary distribution  $\pi$ , let  $T_n > 0$  denote a hitting time for  $[n]^c$ , and let  $X_n = X(T_n)$ . Guy Louchard popularized a conjecture that, for  $n \rightarrow \infty$ ,  $T_n$  is almost Geometric( $p$ ),  $p = \pi([n]^c)$ ,  $X_n$  is almost stationaryly distributed on  $[n]^c$ , and that  $X_n$  and  $T_n$  are almost independent, if  $p(n) := \sup_i p(i, [n]^c) \rightarrow 0$  exponentially fast. For the chains with  $p(n) \rightarrow 0$  however slowly, and with  $\sup_{i,j} \|p(i, \cdot) - p(j, \cdot)\|_{TV} < 1$ , we show that a stronger claim is true for the sequence of hits of any  $S_n \subset \mathbb{N}$  with  $\pi(S_n) \rightarrow 0$ . The conditions are met by the Markov chains that arose in Louchard's studies of two random integer compositions. We show that the chains sharply approximate both compositions. Using a chain approximation and the approximation of the hit sequence for  $[n]^c$ , we study the largest parts of each of the compositions. (Received July 31, 2010)