Let $G$ be a finite (or compact) group acting linearly on a unit sphere. The classification of such actions is usually well understood via the (real) representation theory of $G$. In sharp contrast, the topology of the corresponding quotient spaces is very poorly understood. We will survey a few results and questions in this subject of particular interest to the speaker. (Received August 08, 2010)