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**Grégoire Dupont** and **Hugh Thomas\*** (hthomas@unb.ca). *A geometric interpretation of the transverse quiver Grassmannian*. Preliminary report.

The well-known Laurent phenomenon in cluster algebras states that an element  $g$  of the cluster algebra  $A$  can be expressed as a Laurent polynomial in the cluster variables of any cluster of  $A$ . If  $g$  can always be written as such a Laurent polynomial with *positive* coefficients, then  $g$  is called a “positive” element of  $A$ . A  $\mathbb{Z}$ -basis  $\mathcal{B}$  of a cluster algebra  $A$  is called “canonically positive” if the positive elements of  $A$  are exactly the non-negative linear combinations of elements of  $\mathcal{B}$ . (These notions go back to Sherman-Zelevinsky, 2003.)

Based on the known examples of canonically positive bases due to Sherman-Zelevinsky and Cerulli, Dupont has conjectured a construction of the canonically positive basis in arbitrary finite and affine type, in terms of Euler characteristics of “transverse quiver Grassmannians”. I will report on our attempts to improve the understanding of the conjecture, by interpreting the transverse quiver Grassmannian of submodules of a regular indecomposable  $M$  as the subvariety of the usual quiver Grassmannian consisting of modules which admit deformations locally (with respect to the  $\mathbb{P}^1$  structure of the collection of tubes). (Received August 10, 2010)