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Piotr Hajlasz* (hajlasz@pitt.edu), University of Pittsburgh, Department of Mathematics, 301 Thackeray Hall, Pittsburgh, PA 15260. *Approximation of Sobolev mappings into metric spaces.*

This will be a brief survey of recent results related to the problem of density of Lipschitz mappings in the space of Sobolev mappings from a manifold into a metric space or between metric spaces. The following topics will be discussed:

(1) A complete characterization (in terms of homotopy groups) of Lipschitz polyhedra Y such that for every space X supporting the p -Poincaré inequality, Lipschitz mappings are dense in the space of Sobolev mappings $W^{1,p}(X, Y)$.

(2) The Sobolev space of mappings from a manifold into a metric space $W^{1,p}(M, X)$ can be defined with a help of an isometric embedding of X into a Banach space (for example ℓ^∞). It turns out that the answer to the question whether Lipschitz mappings are dense in the space $W^{1,p}(M, X)$, may depend on the particular choice of the isometric embedding of X .

(3) The problem of approximation of Sobolev mappings into the Heisenberg group by Lipschitz mappings. Connection to Lipschitz homotopy groups of the Heisenberg group. (Received July 21, 2010)