

1063-46-243

Alexander A. Katz* (katza@stjohns.edu), St. John's University, Department of Mathematics & Computer Science, 300 Howard Ave., DaSilva Academic Center 314, Staten Island, NY 10301.

On real \mathbb{B} - C^ -algebras.*

Let A be a real C^* -algebra, and \mathbb{B} be a complete Boolean subalgebra of the Boolean algebra of all central projections of A . We call A a real \mathbb{B} - C^* -algebra, if for each partition of unity $(e_\lambda)_{\lambda \in \Lambda} \in \mathbb{B}$, and each family $(x_\lambda)_{\lambda \in \Lambda} \in A$, there exists a unique \mathbb{B} -mixing $\text{mix}_{\lambda \in \Lambda}(e_\lambda x_\lambda)$, i.e. a unique $x \in A$ such that $e_\lambda x_\lambda = e_\lambda x$ for all $\lambda \in \Lambda$. Let now $\mathbb{V}^{(\mathbb{B})}$ be a Boolean valued universe. Among other basic properties of real \mathbb{B} - C^* -algebras it is established that a bounded descent of a real C^* -algebra inside $\mathbb{V}^{(\mathbb{B})}$ is a real \mathbb{B} - C^* -algebra. Conversely, it is shown that for every real \mathbb{B} - C^* -algebra A there exists a unique (up to a real $*$ -isomorphism) real C^* -algebra \mathcal{A} inside $\mathbb{V}^{(\mathbb{B})}$ whose bounded descent is isometrically real $*$ - \mathbb{B} -isomorphic to A . (Received August 17, 2010)