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A  $(k, d)$ -decomposition of a graph  $G$  is a partition of its edges into  $k$  forests and a graph with maximum degree at most  $d$ . A recent series of papers on  $(1, d)$ -decompositions of planar graphs with a given girth was inspired by the observation of X. Zhu that the game chromatic number and the game coloring number of every  $(1, d)$ -decomposable graph is at most  $4 + d$ . We prove that every graph  $G$  with *maximum average degree*,  $mad(G)$ , less than  $4 - \frac{4}{d+2}$  is  $(1, d)$ -decomposable. The result is sharp (since for every  $d \geq 1$  there are graphs  $G_d$  with  $mad(G_d) = 4 - \frac{4}{d+2}$  that are not  $(1, d)$ -decomposable) and implies several recent results on planar graphs with given girth. We also give a sharp sparseness condition for a graph to be  $(k, d)$ -decomposable when  $k < d$ . (Received September 01, 2010)