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Tao Jiang, Oleg Pikhurko and Zelealem B Yilma* (zyilma@andrew.cmu.edu), Dept. of Mathematical Sciences, Carnegie Mellon University, Pittsburgh, PA 15213. *Set systems without a strong simplex.*

A *d-simplex* is a collection of $d + 1$ sets such that every d of them have non-empty intersection and the intersection of all of them is empty. A *strong d-simplex* is a collection of $d + 2$ sets A, A_1, \dots, A_{d+1} such that $\{A_1, \dots, A_{d+1}\}$ is a d -simplex, while A contains an element of $\cap_{j \neq i} A_j$ for each $i, 1 \leq i \leq d + 1$.

Mubayi and Ramadurai [*Combin. Probab. Comput.*, 18 (2009), pp. 441-454] conjectured that if $k \geq d + 1 \geq 3$, $n > k(d + 1)/d$, and \mathcal{F} is a family of k -element subsets of an n -element set that contains no strong d -simplex, then $|\mathcal{F}| \leq \binom{n-1}{k-1}$ with equality only when \mathcal{F} is a star. We prove their conjecture when $k \geq d + 2$ and n is large. The case $k = d + 1$ was solved in [M. Feng and X. J. Liu, *Discrete Math.*, 310 (2010), pp. 1645-1647]. Our result also yields a new proof of a result of Frankl and Füredi [*J. Combin. Theory Ser. A*, 45 (1987), pp. 226-262] when $k \geq d + 2$ and n is large. (Received September 07, 2010)