

1064-13-226

Lars Winther Christensen, David A Jorgensen, Hamidreza Rahmati, Janet Striuli and Roger Wiegand* (rwiegand@math.unl.edu), 203 Avery Hall, PO Box 880130, Lincoln, NE 68588-0130. *Exact zero divisors and totally acyclic complexes.*

Let (R, \mathfrak{m}, k) be a local ring. A complex

$$\mathbf{F} : \quad \dots \rightarrow F_{n+1} \rightarrow F_n \rightarrow F_{n-1} \rightarrow \dots$$

of finitely generated free R -modules is said to be *totally acyclic* provided both \mathbf{F} and $\text{Hom}_R(\mathbf{F}, R)$ are exact. One way such complexes can arise is from a pair of “exact zero divisors”, that is, a pair x, y of elements of \mathfrak{m} such that $Rx = (0 :_R y)$ and $Ry = (0 :_R x)$. The complex

$$\dots \rightarrow R \rightarrow R \rightarrow R \rightarrow R \rightarrow \dots ,$$

where the maps are alternating multiplications by x and y , is then totally acyclic.

We will discuss the converse: When does the existence of a totally acyclic complex guarantee the existence of a pair of exact zero divisors? More generally, which rings have such pairs? We will focus mainly on the case of Artinian rings. (Received September 09, 2010)