Stable ideals are a class of monomial ideals with a simple combinatorial description. We present a recursive algorithm for generating all saturated strongly stable ideals with a given Hilbert polynomial. It adapts and extends ideas from the Ph.D. thesis *On the combinatorial structure of the Hilbert Scheme* by Alyson Reeves. (Received September 13, 2010)