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**kenneth W johnson\*** (kwj1@psu.edu), Math Department, PSU Abington, 1600 Woodland Road, Abington, PA 19001. *On the existence of simple loops with two non-trivial conjugacy classes*. Preliminary report.

The Paige loop of order 120 has conjugacy classes of orders  $63 = (2^3 - 1)(2^3 + 1)$  (containing elements of order 2) and  $56 = (2^3 - 1)2^3$  (containing elements of order 3). The question of whether this loop is part of a series of simple loops  $Q(n)$  or order  $2^n(2^{n+1} - 1)$  with exactly two non-trivial conjugacy classes of sizes  $(2^n - 1)2^n$  and  $(2^n - 1)(2^n + 1)$  may be interesting to examine. There is no such  $Q(2)$ . This uses the GAP list of primitive groups and the Nagy program which constructs a loop transversal. For  $n = 3$  the Paige loop is the only loop with such classes. If  $Q(4)$  exists it has order  $496 = 16.31$  and classes of orders 240 and 255. There are two primitive groups of degree 496 with suborbits of size 240 and 255.

It seems more likely that a loop would exist for  $n = 5$  of order  $32.63 = 2016$  with classes of order  $31.32 = 992$  and  $31.33 = 1023$ . There are two primitive permutation groups of degree 2016 with suborbits of orders 992 and 1023, of orders  $50027557148216524800 = 2^{30}.3^8.5^2.7^2.11.17.31$  and  $100055114296433049600 = 2^{31}.3^8.5^2.7^2.11.17.31$ . (Received September 09, 2010)