

1064-53-254

Shihshu Walter Wei* (wwei@ou.edu), Department of Mathematics, The University of Oklahoma, Norman, OK 73019. *Conformal, complex, and p -harmonic geometry.*

We recall a smooth map $u : M \rightarrow N$ between Riemannian manifolds is said to be a p -harmonic map, $p \geq 1$ if it is a critical point of p -energy functional E_p , given by $E_p(u) = \int_M |du|^p dv$ with respect to any compactly supported variations, where $|du|$ is the Hilbert-Schmidt norm of the differential du of u , and dv is the volume element of M .

Examples of p -harmonic maps include rigid motions in classical differential geometry, linear transformations in linear algebra, holomorphic maps in complex analysis and in several complex variables (in which $p = 2$), angle-preserving maps between n -dimensional manifolds in conformal geometry (in which $p = n$), geodesics, (conformal) minimal submanifolds (for every $p \geq 1$), harmonic maps (in which $p = 2$), and much more.

We'll explore several natural links between the geometry of p -harmonic maps, conformal geometry, and complex geometry. Some applications to topology and partial differential equations will be considered. (Received September 11, 2010)