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It is well known that every graph G contains a bipartite subgraph H with at least half the edges of G . The standard “pushing” argument shows that in fact the degree of each vertex in H is at least half its degree in G . A linearity of expectation argument also shows that a spanning balanced bipartite subgraph exists with at least half the edges. Can both properties be simultaneously obtained? That is, does there exist a spanning balanced bipartite subgraph H of G such that the degree of each vertex in H is at least half its degree (rounded down) in G ? Bollobás and Scott have conjectured that this is in fact true. We will discuss partial results on this question, including probabilistic approaches and a potential version: for any degree sequence π , we show that there exists a realization G of π that has a bipartite subgraph H with (almost) the desired properties. (Received September 12, 2010)