

1065-12-168

**Thomas J. Tucker\*** (tjtucker@gmail.com), Math Department, University of Rochester,  
Rochester, NY 14610. *P-adic parametrization of orbits.*

Let  $f : X \rightarrow X$  be a morphism of varieties over a field of characteristic 0 and let  $x$  be a point on  $X$ . In many cases, one can show the orbit of  $x$  under  $f$  can be "p-adically parametrized"; that is, one can find a p-adic analytic map  $g$  from a disc in  $\mathbb{C}_p$  to  $X$  such that  $g(n) = f^n(x)$  for all  $n$ . The existence of such a parametrization allows one to solve the so-called "dynamical Mordell-Lang problem" for  $f$ , which states that, given a subvariety  $W$  of  $X$ , the set of  $n$  such that  $f^n(x)$  is in  $W$  forms a finite union of arithmetic sequences. It also allows for the solution of various weak forms of a conjecture of Zhang on the existence of points with Zariski dense orbits. (Received September 12, 2010)