

In 2004 Dowling, Lennard and Turett showed that every non-weakly compact, closed, bounded, convex (c.b.c.) subset  $K$  of  $(c_0, \|\cdot\|_\infty)$  is such that there exists a  $\|\cdot\|_\infty$ -nonexpansive mapping  $T$  on  $K$  that is fixed point free. This mapping  $T$  is generally not affine. We prove that if a Banach space contains an asymptotically isometric (ai)  $c_0$ -summing basic sequence  $(x_n)_{n \in \mathbb{N}}$ , then the closed convex hull of  $(x_n)_{n \in \mathbb{N}}$ ,  $E := \overline{\text{co}}(\{x_n : n \in \mathbb{N}\})$ , fails the fixed point property for affine nonexpansive mappings. Also, there exists an *affine contractive* mapping  $U : E \rightarrow E$  that is fixed point free. We conclude

for  $\vec{b} = (b_n)_{n \in \mathbb{N}}$  in  $\mathbb{R}$  s.t.

$$0 < m := \inf_{n \in \mathbb{N}} b_n \text{ and } M := \sup_{n \in \mathbb{N}} b_n < \infty$$

The c.b.c. subset  $E$ ,

$$E := \left\{ \sum_{n=1}^{\infty} t_n f_n : 1 = t_1 \geq t_2 \geq \cdots \geq t_n \downarrow_n 0 \right\} .$$

where  $f_n := b_n e_n$ , for all  $n \in \mathbb{N}$ , fails the fpp (affine, n.e.).

Note that this applies to  $b_n = r_n$ , where  $(r_n)_{n \in \mathbb{N}}$  is an enumeration of  $[m, M)$ ,  $\forall 0 < m < M < \infty$ .

(Received September 14, 2010)