

1065-70-33

**Tiancheng Ouyang** and **Zhifu Xie\*** (zxie@vsu.edu), Department of Math. & Computer Science, P.O.Box 9068, Virginia State University, Petersburg, VA 23806. *Number of Central Configurations in the Collinear Four-body Problem.*

For a given  $m = (m_1, m_2, \dots, m_n) \in (\mathbf{R}^+)^n$ , let  $p$  and  $q \in (\mathbf{R}^d)^n$  be two central configurations for  $m$ . Then we call  $p$  and  $q$  *geometrically equivalent* and write  $p \sim q$  if they differ by a rotation followed by a scalar multiplication as well as by a permutation of bodies. Denote by  $L(n, m)$  the set of geometric equivalence classes of  $n$ -body collinear central configurations for any given mass vector  $m$ . There are other different understandings of equivalence of central configurations in collinear  $n$ -body problem. Under the usual definition of equivalence of central configurations in history, permutations of the bodies are not allowed and we call them *permutation equivalence*. In this case Euler found three collinear central configurations and Moulton generalized to  $n!/2$  central configurations for any given mass  $m$  in the collinear  $n$ -body problem under permutation equivalence. The main result in this paper is the discovery of the explicit parametric expressions of the union  $H_4$  of the singular surfaces in the mass space  $m \in (\mathbf{R}^+)^4$ . We prove that the number of central configurations  $\#L(4, m) = 4!/2 - 1 = 11$  if  $m_1, m_2, m_3$  and  $m_4$  are mutually distinct and  $m \in H_4$ . (Received August 06, 2010)