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Peter W Bates (bates@math.msu.edu), Department of Mathematics, Michigan State University, East Lansing, MI 48824, and Chunlei Zhang* (zhangc@suu.edu), Department of Mathematics, Southern Utah University, 351 W. University Blvd., Cedar City, UT 84720. Traveling Pulses for the Nonlocal and Lattice Klein-Gordon Equations.

We study traveling pulses on a lattice and in a continuum where all pairs of particles interact, contributing to the potential energy. The interaction may be positive or negative, depending on the particular pair but overall is positive in a certain sense. For such an interaction kernel J with unit integral (or sum), the operator $\frac{1}{\varepsilon^2}[J*u-u]$, with * continuous or discrete convolution, shares some common features with the spatial second derivative operator, especially when ε is small. Therefore, the equation $u_{tt} - \frac{1}{\varepsilon^2}[J*u-u] + f(u) = 0$ may be compared with the nonlinear Klein Gordon equation $u_{tt} - u_{xx} + f(u) = 0$. If f is such that the Klein-Gordon equation has supersonic traveling pulses, we show that the same is true for the nonlocal version, both the continuum and lattice cases. (Received August 12, 2006)