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Keith Burns* (burns@math.northwestern.edu), Department of Mathematics, Northwestern University, Evanston, IL 60208, and Benjamin Schmidt (bischmid@uchicago.edu), Department of Mathematics, University of Chicago, Chicago, IL 60637. Conjugate points and non injectivity of the exponential map.

It is well known that if $v \in T_pM$ is a vector such that p and $q = \exp_p(v)$ are conjugate along the geodesic tangent to v, then \exp_p is non injective in any neighbourhood of v. This means one can find geodesics starting at p with initial tangent vectors v' and v'' close to v that intersect close to q.

Ben Schmidt and I have sharpened this result by showing that can always choose one of the vectors v' and v'' to be v. (Received January 12, 2009)