

Meeting: 999, Nashville, Tennessee, SS 4A, Special Session on Universal Algebra and Lattice Theory

999-08-135 **Kira Adaricheva*** (kadaricheva@ccc.edu), Harold Washington College, 30 East Lake St., Chicago, IL 60601, and **Agata Pilitowska**, Warsaw University of Technology. *Complex Algebras of Subalgebras*. Preliminary report.

The complex algebra of subsets of an algebra G is the algebra of the same type defined on the set of all non-empty subsets of the carrier of G . When we consider only non-void subalgebras of G we obtain the notion of the complex algebra SG of subalgebras. Evidently, the complex algebra of subalgebras is not always defined for an arbitrary algebra G .

We describe the necessary and sufficient condition, called *the complex condition*, for a variety V to ensure that the complex algebra of subalgebras is defined for any algebra from V .

G.Grätzer and H.Lakser proved that the variety $VUS(G)$ generated by all algebras of subsets for the algebras from $V(G)$ coincides with $V(G)$ iff G is defined by linear identities.

Now assume that the complex condition holds in $V(G)$, thus the variety $VS(G)$ generated by complex algebras of subalgebras of algebras from $V(G)$ is defined. The question, whether $VS(G) = V(G)$ implies that G is defined by linear or idempotent identities, is still open. We show that the premise of this conjecture cannot be replaced with the weaker condition that SG is defined and $V(SG) = V(G)$.

We also investigate the suprising conjecture that the complex condition might be equivalent to the entropic law. (Received August 19, 2004)