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2017

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МАТЕМАТИЧЕСКОГО
ОБЩЕСТВА

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Translation edited by Frances H. Goldman
with the assistance of AMS staff

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ТРУДЫ МОСКОВСКОГО МАТЕМАТИЧЕСКОГО ОБЩЕСТВА

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Congratulations to Ernest Borisovich Vinberg
on his 80th birthday anniversary

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