

PROCEEDINGS
OF THE
AMERICAN MATHEMATICAL SOCIETY

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VOLUME 11, NUMBER 5
OCTOBER, 1960

PUBLISHED BY THE SOCIETY
MENASHA, WIS., AND PROVIDENCE, R. I.

Journals Published by the American Mathematical Society

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Papers in algebra and number theory should be sent to ALEX ROSENBERG, Department of Mathematics, University of California, Berkeley 4, California; in probability, real variables, logic, and foundations to P. R. HALMOS, Eckhart Hall, University of Chicago, Chicago 37, Illinois; in abstract analysis to either P. R. HALMOS or ALEX ROSENBERG; in geometry and topology to HANS SAMELSON, Institute for Advanced Study, Princeton, N. J.; in other branches of analysis, applied mathematics, and all other fields to R. P. BOAS, Lunt Building, Northwestern University, Evanston, Illinois. All other communications to the editors should be addressed to the Managing Editor, P. R. HALMOS.

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Second-class postage paid at Menasha, Wisconsin. Authorization is granted under the authority of the act of August 24, 1912, as amended by the act of August 4, 1947 (sec. 34.21, P. L. & R.). Acceptance for mailing at the special rate of postage provided for in section 34.40, paragraph d., P. L. & R.

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