

fined on the real line X is an example of a function which is locally an ϵ -mapping in the narrow sense, but which is not a polynomial mapping. In this case we have $f(X) \neq X$.

REMARK 2. From Theorem 3 it follows that if F satisfies the assumptions of Theorem 3, then there exists a point x such that $F(x) = x$ (i.e., $F: X \rightarrow X$ has a fixed point).

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A CHAINABLE CONTINUUM NO TWO OF WHOSE NONDEGENERATE SUBCONTINUA ARE HOMEOMORPHIC

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R. D. Anderson and Gustave Choquet [1] gave an example of a plane continuum no two of whose nondegenerate subcontinua are homeomorphic. The object of this note is to point out that there is a chainable continuum having this property. The only change we make in the construction given in [1] is to replace the n -ods used by R. D. Anderson and Gustave Choquet by chainable continua C_{n-2} .

A subcontinuum Y of a continuum X is a separating continuum of X if $X - Y$ is not connected and $\text{Cl}(X - Y) = X$. A subcontinuum Y of a continuum X is a strong separating continuum if:

- (1) Y is a separating continuum of X ,
- (2) $X - Y$ has two components, X_1 and X_2 ,
- (3) there are points $y_1, y_2 \in Y$ such that $y_i \in \text{Cl}(X_i)$.

Let $V = \{(x, y)/y = |x| \text{ and } -1 < x < 1\}$. Let C_n be formed from n copies of V and $n+1$ "lines" so that each V is a strong separating continuum of C_n as in Figure 1 (for $n = 2$).

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FIGURE 1

Following [1] we construct a continuum X using C_n in place of the $(n+2)$ -ods used in [1]. As in [1], if A and B are subcontinua of X we may assume $A - B$ is not empty and hence $A - B$ contains a separating continuum Y of A . Now Y contains k strong separating continua. No subcontinuum of B has this property. Hence A and B are not homeomorphic.

In order to show that X is chainable we first note that each M_i is chainable.

By Lemma 2 of [1] we have the following: For each number $\epsilon > 0$ there is an integer i such that $D(\tilde{f}_i^{-1}(p)) < \epsilon$, for $p \in M_i$ and \tilde{f}_i the map induced by $f_j: M_{j+1} \rightarrow M_j$ of X onto M_i . This implies that there is a $\delta > 0$ such that if U is open in M_i and $D(U) < \delta$, then $D(\tilde{f}_i^{-1}(U)) < \epsilon$.

One need only assume the contrary. Then for each $\delta > 0$ there is a $U(\delta)$ such that $D(U(\delta)) < \delta$ and $D(\tilde{f}_i^{-1}(U(\delta))) > \epsilon$. Let p be a limit point of a set P of points $p_j \in U(1/j)$. If U is an open set containing p then $U \supset U(1/j)$ for some j and hence $D(\tilde{f}_i^{-1}(p)) > \epsilon$. But this contradicts our choice of M_i . In order to ϵ -chain X we need only δ -chain M_i .

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